

MATH

(BENGALI Version)

1. $\frac{x^2}{144} + \frac{y^2}{25} = 1$. উপরের নাভিগামী যে বৃত্তের কেন্দ্র $(0, \sqrt{2})$ বিন্দুতে তার ব্যাসার্ধ হচ্ছে —
 (A) 9 (B) 7 (C) 11 (D) 5
2. $\triangle ABC$ একটি ত্রিভুজ $\tan A, \tan B$ হল $pq(x^2+1)=r^2x$ সমীকরণের দুটি বীজ। তাহলে $\triangle ABC$ হবে—
 (a) সমকোণী ত্রিভুজ (b) সূক্ষ্মকোণী ত্রিভুজ (c) স্থূলকোণী ত্রিভুজ (d) সমবাহু ত্রিভুজ
3. A এবং B সেটে যথাক্রমে p ও q সংখ্যক element আছে। তাহলে সেট A থেকে সেট B এর মধ্যে সম্পর্ক (relation) এর সংখ্যা—
 (A) 2^{p+q} (B) 2^{pq} (C) $p+q$ (D) pq
4. যদি জটিল তলে z_1, z_2 দুটি নির্দিষ্ট বিন্দু এবং z একটি যে কোনো বিন্দু হয় এবং $|z - z_1| + |z - z_2| = 2|z_1 - z_2|$ হয় তাহলে z বিন্দুর সঞ্চারণ পথ—
 (A) একটি উপবৃত্ত (B) z এবং z_2 বিন্দু সংযোগকারী একটি সরলরেখা
 (C) একটি অধিবৃত্ত (D) z_1 এবং z_2 বিন্দু সংযোগকারী সরলরেখার সমদ্বিখণ্ডক।
5. যদি $S = \frac{2}{1} {}^n C_0 + \frac{2^2}{2} {}^n C_1 + \frac{2^3}{3} {}^n C_2 + \dots + \frac{2^{n+1}}{n+1} {}^n C_n$ হয় তাহলে S সমান
 (A) $\frac{2^{n-1} - 1}{n+1}$ (B) $\frac{3^{n+1} - 1}{n+1}$ (C) $\frac{3^n - 1}{3}$ (D) $\frac{2^n - 1}{n}$
6. 7টি consonant এবং 4টি vowel-এর মধ্যে থেকে 3টি consonant ও 2টি vowel নিয়ে কয়টি অর্থপূর্ণ শব্দ গঠন করা যাবে।
 (A) 24800 (B) 25100 (C) 25200 (D) 25400
7. $1!+2!+3!+\dots+11!$ কে 12 দিয়ে ভাগ করলে ভাগশেষ হয় —
 (A) 9 (B) 8 (C) 7 (D) 6
8. যে কোনো বাস্তব সংখ্যা x-এর জন্য $f(x) = \frac{x}{1!} + \frac{3}{2!}x^2 + \frac{7}{3!}x^3 + \frac{15}{4!}x^4 + \dots$ $f(x)=0$ সমীকরণের
 (A) কোনো বাস্তব সমাধান নেই (B) কেবলমাত্র একটি বাস্তব সমাধান আছে
 (C) কেবলমাত্র দুটি বাস্তব সমাধান আছে (D) অসংখ্য বাস্তব সমাধান আছে
9. যদি $x^2 + px + q = 0$ সমীকরণের α, β দুটি বীজ হয় তাহলে $\alpha^3 + \beta^3$ এবং $\alpha^4 + \alpha^2\beta^2 + \beta^4$ -এর মান যথাক্রমে
 (A) $3pq - p^3$ এবং $p^4 - 3p^2q + 3q^2$ (B) $-p(3q - p^2)$ এবং $(p^2 - q)(p^2 + 3q)$
 (C) $pq - 4$ এবং $p^4 - q^4$ (D) $3pq - p^3$ এবং $(p^2 - q)(p^2 - 3q)$

10. একটি ঝাঁকশূন্য ছকা কে 12 বার নিক্ষেপ করা হোল। প্রতিটি face দু'বার করে পড়ার সম্ভাবনা হোল—

- (A) $\frac{12!}{6!6!6^{12}}$ (B) $\frac{2^{12}}{2^6 6^{12}}$ (C) $\frac{12!}{2^6 6^{12}}$ (D) $\frac{12!}{2^6 6^{12}}$

11. $\tan \frac{\pi}{5} + 2 \tan \frac{2\pi}{5} + 4 \cot \frac{4\pi}{5}$ -এর মান

- (A) $\cot \frac{\pi}{5}$ (B) $\cot \frac{2\pi}{5}$ (C) $\cot \frac{4\pi}{5}$ (D) $\cot \frac{3\pi}{5}$

12. $y = x^2$ এবং $x = y^2$ বক্র দ্বারা সীমাবদ্ধ ক্ষেত্রের ক্ষেত্রফল —

- (A) $1/3$ (B) $1/2$ (C) $1/4$ (D) 3

13. $4x+3y+35=0$ সরলরেখার নিকটবর্তী এবং $y^2 = 64x$ অধিবৃত্তের উপর অবস্থিত বিন্দুর স্থানাঙ্ক—

- (A) $(9, -24)$ (B) $(1, 81)$ (C) $(4, -16)$ (D) $(-9, -24)$

14. $({}^n C_1)^2 + ({}^n C_2)^2 + ({}^n C_3)^2 \dots + ({}^n C_n)^2$ -এর মান

- (A) $({}^{2n} C_n)^2$ (B) ${}^{2n} C_n$ (C) ${}^{2n} C_n + 1$ (D) ${}^{2n} C_n - 1$

15. কোনো পরিবারে 2 জন শিশুর মধ্যে 1 জন বালক। দ্বিতীয় শিশুটি বালিকা হওয়ার সম্ভাবনা —

- (A) $1/2$ (B) $1/3$ (C) $2/3$ (D) $7/10$

16. 20^{301} সংখ্যাটিতে অঙ্কে সংখ্যা (যেখানে $\log_{10} 2 = 0.3010$)

- (A) 602 (B) 301 (C) 392 (D) 391

17. যদি $\sqrt{y} = \cos^{-1} x$, $(1-x^2) \frac{d^2 y}{dx^2} - x \frac{dy}{dx} = c$ অবকল সমীকরণকে সিদ্ধ করে তাহলে c-এর

মান —

- (A) 0 (B) 3 (C) 1 (D) 2

18. $(1+x^2) \frac{dy}{dx} + y = e^{\tan^{-1} x}$ অবকল সমীকরণের সমাকল গুণাঙ্ক (I. F) —

- (A) $\tan^{-1} x$ (B) $1+x^2$ (C) $e^{\tan^{-1} x}$ (D) $\log_e(1+x^2)$

19. $\log_{10} \log_7 (\sqrt{x+7} + \sqrt{x}) = 0$ সমীকরণের সমাধান

- (A) 3 (B) 7 (C) 9 (D) 49

20. যদি $f(x)$ একটি অন্তরকলনযোগ্য অপেক্ষক হয় এবং $f(4) = 5$ হয় তাহলে


$$= \lim_{x \rightarrow 2} \frac{f(4) - f(x)^2}{x-2} \text{ এর মান}$$

- (A) 0 (B) 5 (C) 20 (D) -20

21. $\lim_{x \rightarrow 0} \frac{\int_0^{x^2} \cos(t^2) dt}{x \sin x}$ -এর মান
 (A) 1 (B) -1 (C) 2 (D) $\log_e 2$
22. $\sqrt{x+1} - \sqrt{x-1} = \sqrt{4x-1}$ সমীকরণের সমাধান সংখ্যা
 (A) 2 (B) 0 (C) 3 (D) 1
23. যদি $\lim_{x \rightarrow 0} \frac{2a \sin x - \sin 2x}{\tan^3 x} = 1$ হয় তাহলে a এর মান
 (A) 2 (B) 1 (C) 0 (D) -1
24. যদি $f(x) = \begin{cases} 2x^2 + 1, & x \leq 1 \\ 4x^3 - 1, & x > 1 \end{cases}$ হয়, তাহলে $\int_0^2 f(x) dx$ -এর মান
 (A) 47/3 (B) 50/3 (C) 1/3 (D) 47/2
25. যদি $\sin^{-1}\left(\frac{x}{13}\right) + \operatorname{cosec}^{-1}\left(\frac{13}{12}\right) = \frac{\pi}{2}$ হয়, তবে x -এর মান —
 (A) 5 (B) 4 (C) 12 (D) 11

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.... and so on



1

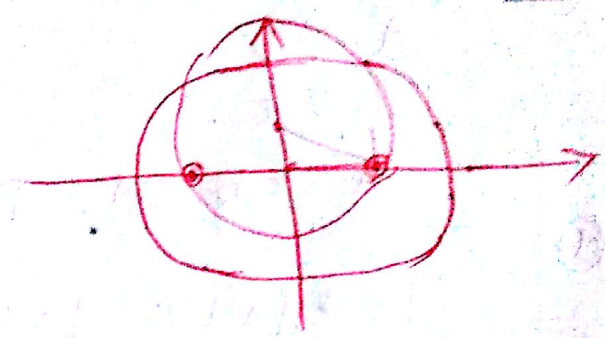
Q. No.

$$\frac{x^2}{144} + \frac{y^2}{25} = 1$$

$$\Rightarrow \frac{x^2}{(12)^2} + \frac{y^2}{5^2} = 1$$

$$\Rightarrow a=12, b=5$$

इष्टतम बिन्दु $(0, \sqrt{a}) \Rightarrow$



$$\therefore \text{Eccentricity } e = \sqrt{1 - \frac{b^2}{a^2}} = \sqrt{1 - \frac{25}{144}} = \sqrt{\frac{144 - 25}{144}} = \frac{\sqrt{119}}{12}$$

$$\therefore ae = \frac{\sqrt{119}}{12} \times 12 = \sqrt{119}$$

$$\therefore \text{अवसाद} = \sqrt{(\sqrt{119})^2 + (5)^2} = \sqrt{119 + 25} = \sqrt{144} = 12$$

Option (C)

2

$$pqm^2 - n^2m + pq = 0$$

$$\Rightarrow m = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{n^2 \pm \sqrt{n^4 - 4 \cdot p \cdot q}}{2pq}$$

$$= \frac{n^2 \pm \sqrt{n^4 - 4pq}}{2pq}$$

~~Option~~

$$\therefore \tan A + \tan B =$$

$$\tan A \cdot \tan B = 1$$

$$\begin{cases} a+b = \frac{n^2}{pq} \\ ab = \frac{pq}{pq} = 1 \end{cases}$$

$$\Rightarrow \tan A = \cot B$$

$$\Rightarrow \tan A = \tan\left(\frac{\pi}{2} - B\right)$$

$$\Rightarrow A + B = \frac{\pi}{2}$$

सहायकी त्रिकोण

Option (A)



3

Q.
No.

$$A \rightarrow p$$

$$B \rightarrow q$$

$A \rightarrow B$ সত্য. $p \wedge q$ Option **(D)**.

4

$$|z - z_1| + |z - z_2| = 2|z_1 - z_2|$$

$$z = x + iy, \quad z_1 = x_1 + iy_1$$

$$z_2 = x_2 + iy_2$$

$$\Rightarrow |x + iy - (x_1 + iy_1)| + |x + iy - (x_2 + iy_2)|$$

$$= 2|(x_1 - x_2) + i(y_1 - y_2)|$$

$$\Rightarrow \sqrt{(x - x_1)^2 + (y - y_1)^2} + \sqrt{(x - x_2)^2 + (y - y_2)^2}$$

$$= 2\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

$$\Rightarrow (x - x_1)^2 + (y - y_1)^2 + 2\left\{[(x - x_1) + (y - y_1)]\left[(x - x_2) + (y - y_2)\right]\right\}$$

$$+ (x - x_2)^2 + (y - y_2)^2 = 4\left\{(x_1 - x_2)^2 + (y_1 - y_2)^2\right\}$$

$$\Rightarrow x^2 - 2xx_1 + x_1^2 + y^2 - 2yy_1 + y_1^2 + 2(x - x_1)(x - x_2) + 2(x - x_1)(y - y_2)$$

$$+ 2(y - y_1)(x - x_2) + 2(y - y_1)(y - y_2) + x_2^2 - 2xx_2 + x_2^2 + y^2 - 2yy_2$$

$$+ y_2^2 = 4\left\{x_1^2 + x_2^2 - 2x_1x_2 + y_1^2 + y_2^2 - 2y_1y_2\right\}$$

৷





5

Q. No.

$$S = \frac{2}{1} \cdot nC_0 + \frac{2^2}{2} nC_1 + \frac{2^3}{3} nC_2 + \dots + \frac{2^{n+1}}{n+1} nC_n$$

$$= \frac{2^{n+1} - 1}{n+1} \checkmark$$

6

$${}^7C_3 \times {}^4C_2$$

$$= \frac{7!}{3!4!} \times \frac{4!}{2!2!}$$

$$= \frac{7 \times 6 \times 5 \times 4!}{3 \times 2 \times 4!} \times \frac{3 \times 4 \times 2!}{2!2!}$$

$$= \frac{35 \times 6}{210}$$

$${}^7P_3 \times {}^4P_2$$

$$= \frac{7!}{(7-3)!} \times \frac{4!}{(4-2)!}$$

$$= \frac{7 \times 6 \times 5 \times 4!}{4!} \times \frac{4 \times 3 \times 2!}{2!}$$

$$= 30 \times 7 \times 12$$

$$= 360 \times 7$$

$$= 2520$$

7

$$1! + 2! + 3! + \dots + 11!$$

$$= 43954713$$

(A) 9

[n(n+1)]

8

$$f(x) = \frac{x}{1!} + \frac{3}{2!} x^2 + \frac{7}{3!} x^3 + \frac{15}{3!} x^4 + \dots$$

$$= \frac{x}{1!} + \frac{1+2}{2!} x^2 + \frac{2^2+3}{3!} x^3 + \frac{3^2+6}{3!} x^4 + \dots$$

सही तरह का राशियाँ ज्ञात करें (A)

9

$$\alpha + \beta = -b$$

$$\alpha\beta = c$$

$$\therefore \alpha^3 + \beta^3 = (\alpha + \beta)(\alpha^2 + \beta^2 + \alpha\beta)$$

$$= (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta)$$

$$= -b^3 + 3c b = 3cb - b^3$$



9.
No.

$$\begin{aligned}
 & \alpha^4 + \beta^4 + \alpha^2\beta^2 \\
 &= (\alpha^2 + \beta^2)^2 - 2\alpha^2\beta^2 + \alpha^2\beta^2 \\
 &= ((\alpha + \beta)^2 - 2\alpha\beta)^2 - \alpha^2\beta^2 \\
 &= (p^2 - 2q)^2 - q^2 \\
 &= (p^2 - q)(p^2 - 3q)
 \end{aligned}$$

 $\pi - 2$

10

Option (B)

11

$$\begin{aligned}
 & \tan \frac{\pi}{5} + 2 \tan \frac{2\pi}{5} + 4 \cot \frac{4\pi}{5} \\
 &= \tan \frac{\pi}{5} + \tan \frac{2\pi}{5} + \tan \frac{2\pi}{5} + 4 \cot \frac{4\pi}{5} \\
 &= \cancel{\tan \frac{\pi}{5}} - \cot \frac{4\pi}{5} + \tan \frac{2\pi}{5} = \cot 2\pi \\
 &= \tan \frac{\pi}{5} + \tan \frac{2\pi}{5} + \tan \frac{2\pi}{5} + 4 \cot (\pi - \frac{\pi}{5}) \\
 &= \tan \frac{\pi}{5} + \tan \frac{2\pi}{5} + \tan \frac{2\pi}{5} - 4 \cot \frac{\pi}{5}
 \end{aligned}$$

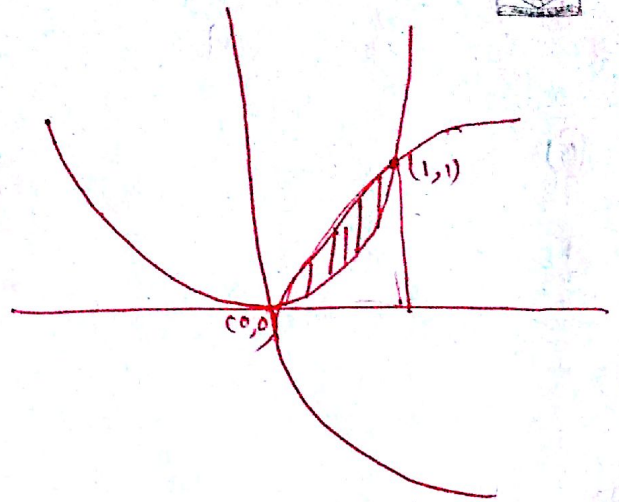




12

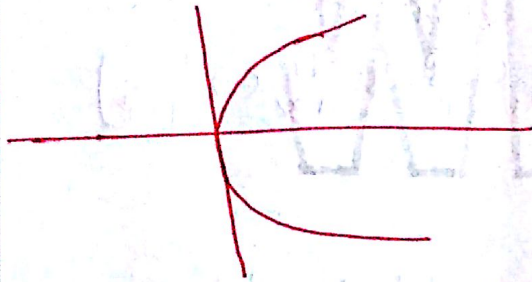
Q.
No.

$$\begin{aligned}
 y &= x^2, \quad x = y \\
 \therefore \int_0^1 y dx - \int_0^1 x dy \\
 &= \int_0^1 x^2 dy - \int_0^1 y^2 dy \\
 &= \left[\frac{x^3}{3} \right]_0^1 - \left[\frac{y^3}{3} \right]_0^1 \\
 &= \frac{1}{3} + \frac{1}{3} = \frac{2}{6} = \frac{1}{3}
 \end{aligned}$$



13

$$4x + 3y + 35 = 0$$



$$y^2 = 64x$$

$$y^2 = 4ax$$

$$\therefore 4a = 64 \Rightarrow a = 16$$

14

$$\begin{aligned}
 &1^2 + 2^2 + 3^2 + \dots + n^2 \\
 &= \frac{n(n+1)(2n+1)}{6} \\
 &= \frac{n \cdot n (n+1) [2n+1]}{6} \\
 &=
 \end{aligned}$$





15

Q
No.

16

 $\frac{1}{2}$ (A)

17

$$\sqrt{y} = \cos^{-1}x \Rightarrow y = (\cos^{-1}x)^2$$

$$\therefore \frac{dy}{dx} = 2 \cos^{-1}x \cdot \frac{-1}{\sqrt{1-x^2}}$$

$$\frac{d^2y}{dx^2} = 2 \cdot y \cdot \left[\frac{-(-2x)}{2\sqrt{1-x^2}} + \frac{dy}{dx} \cdot \left(-\frac{1}{\sqrt{1-x^2}}\right) \right]$$

$$\Rightarrow (1-x^2) y'' = 4y$$

$$\Rightarrow (1-x^2) \cdot 2y_1 y_2 + y_1^2 \cdot (-2x) = 4y_1$$

$$\Rightarrow (1-x^2) y_2 - x y_1 = 2$$

$$(1-x^2) y_1^2 = 4y$$

Option (D).

18

$$(1+x^2) \frac{dy}{dx} + y = e^{\tan^{-1}x}$$

$$\Rightarrow \frac{dy}{dx} + \frac{y}{1+x^2} = \frac{e^{\tan^{-1}x}}{1+x^2}$$

$$\text{IF} = e^{\int \frac{1}{1+x^2} dx} = e^{\tan^{-1}x}$$

Integrating factor is $e^{\tan^{-1}x}$





(19)

$$\log_{101} \log_7 (\sqrt{x+7} + \sqrt{x}) = 0$$

$$\log_{101} (\log_7 (\sqrt{x+7} + \sqrt{x})) = \log_{101} 101$$

$$\Rightarrow \log_7 (\sqrt{x+7} + \sqrt{x}) = 101$$

$$\Rightarrow (\sqrt{x+7} + \sqrt{x}) = \dots$$

20.

$$\begin{aligned} f(4) = 5, \quad \lim_{x \rightarrow 2} \frac{f(4) - f(x)^2}{x-2} \\ = \lim_{x \rightarrow 2} \frac{5 - (f(x))^2}{x-2} \\ = \lim_{x \rightarrow 2} \frac{-2f(x) \cdot f'(x)}{1} \\ = -2f(2) \cdot f'(2) \end{aligned}$$





(21)

$$\lim_{x \rightarrow 0} \int_0^x \frac{\cos(x) dx}{x \sin x}$$

Q. No.

(22)

$$\sqrt{x+1} - \sqrt{x-1} = \sqrt{4x-1}$$

$$\Rightarrow x+1 + (x-1) - 2\sqrt{(x+1)(x-1)} = 4x-1$$

$$\Rightarrow 2x - 2\sqrt{(x+1)(x-1)} = 4x-1$$

$$\Rightarrow -2\sqrt{(x+1)(x-1)} = 4x-1 - 2x$$

$$\Rightarrow -2\sqrt{(x+1)(x-1)} = \cancel{4x-3} - 2x - 1$$

$$\Rightarrow (-2\sqrt{x^2-1})^2 = (2x-1)^2$$

$$\Rightarrow 4(x^2-1) = 4x^2 - 2 \cdot 2x \cdot 1 + 1$$

$$\Rightarrow 4x^2 - 4 = 4x^2 - 4x + 1$$

$$\Rightarrow +4x = +5$$

$$\Rightarrow x = 5/4$$

(23)

$$\int_0^2 f(x) dx = \int_0^1 (2x^2+1) dx + \int_1^2 (4x^3-1) dx$$

$$= \left[\frac{2x^3}{3} + x \right]_0^1 + \left[\frac{4x^4}{4} - x \right]_1^2$$

$$= \frac{2}{3} + 1 + 16 - 2 - 1 + 1$$

$$= 17 + \frac{2}{3} - 2 = \frac{51+2-6}{3} = \frac{47}{3}$$

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MATH

(ENGLISH Version)

1. Let the equation of an ellipse be $\frac{x^2}{144} + \frac{y^2}{25} = 1$. Then the radius of the circle with centre $(0, \sqrt{2})$ and passing through the foci of the ellipse is—
 (A) 9 (B) 7 (C) 11 (D) 5
2. In a $\triangle ABC$, $\tan A$ and $\tan B$ are the roots of $pq(x^2+1)=r^2x$. Then $\triangle ABC$ is—
 (A) a right angled triangle (B) an acute angled triangle
 (C) an obtuse angled triangle (D) an equilateral triangle
3. Let the number of elements of the sets A and B be p and q respectively. Then the number of relations from the set A to the set B is—
 (A) 2^{p+q} (B) 2^{pq} (C) $p+q$ (D) pq
4. Let z_1, z_2 be two fixed complex numbers in the Argand plane and z be an arbitrary point satisfying $|z - z_1| + |z - z_2| = 2|z_1 - z_2|$. Then the locus of z will be—
 (A) an ellipse (B) a straight line joining z_1 and z_2
 (C) a parabola (D) a bisector of the line segment joining z_1 and z_2
5. Let $S = \frac{2}{1} {}^n C_0 + \frac{2^2}{2} {}^n C_1 + \frac{2^3}{3} {}^n C_2 + \dots + \frac{2^{n+1}}{n+1} {}^n C_n$. Then S equals
 (A) $\frac{2^{n+1} - 1}{n+1}$ (B) $\frac{3^{n+1} - 1}{n+1}$ (C) $\frac{3^n - 1}{n}$ (D) $\frac{2^n - 1}{n}$
6. Out of 7 consonants and 4 vowels, the number of words (not necessarily meaningful) that can be made, each consisting of 3 consonants and 2 vowels, is
 (A) 24800 (B) 25100 (C) 25200 (D) 25400
7. The remainder obtained when $1!+2!+3!+\dots+11!$ is divided by 12 is
 (A) 9 (B) 8 (C) 7 (D) 6
8. For every real number x , let $f(x) = \frac{x}{1!} + \frac{3}{2!}x^2 + \frac{7}{3!}x^3 + \frac{15}{4!}x^4 + \dots$. Then the equation $f(x)=0$ has
 (A) no real solution (B) exactly one real solution
 (C) exactly two real solutions (D) infinite number of real solutions.
9. If α, β are the roots of the quadratic equation $x^2+px+q=0$, then the values of $\alpha^3 + \beta^3$ and $\alpha^4 + \alpha^2\beta^2 + \beta^4$ are respectively—
 (A) $3pq-p^3$ and $p^4 - 3p^2q + 3q^2$ (B) $-p(3q-p^2)$ and $(p^2-q)(p^2+3q)$
 (C) $pq-4$ and p^4-q^4 (D) $3pq-p^3$ and $(p^2-q)(p^2-3q)$

10. A fair six faced die is rolled 12 times. The probability that each face turns up twice is equal to

- (A) $\frac{12!}{6!6!6^{12}}$ (B) $\frac{2^{12}}{2^6 6^{12}}$ (C) $\frac{12!}{2^6 6^{12}}$ (D) $\frac{12!}{2^6 6^{12}}$

11. The value of $\tan \frac{\pi}{5} + 2 \tan \frac{2\pi}{5} + 4 \cot \frac{4\pi}{5}$ is

- (A) $\cot \frac{\pi}{5}$ (B) $\cot \frac{2\pi}{5}$ (C) $\cot \frac{4\pi}{5}$ (D) $\cot \frac{3\pi}{5}$

12. The area of the region bounded by the curves $y = x^2$ and $x = y^2$ is

- (A) $1/3$ (B) $1/2$ (C) $1/4$ (D) 3

13. The point on the parabola $y^2 = 64x$ which is nearest to the line $4x + 3y + 35 = 0$ has coordinates -

- (A) $(9, -24)$ (B) $(1, 81)$ (C) $(4, -16)$ (D) $(-9, -24)$

14. The value of the sum ${}^n C_1^2 + {}^n C_2^2 + \dots + {}^n C_n^2$ is

- (A) $({}^{2n} C_n)^2$ (B) ${}^{2n} C_n$ (C) ${}^{2n} C_n + 1$ (D) ${}^{2n} C_n - 1$

15. Ram is visiting a friend. Ram knows that his friend has 2 children and 1 of them is a boy. Assuming that a child is equally likely to be a boy or a girl, then the probability that the other child is a girl, is

- (A) $1/2$ (B) $1/3$ (C) $2/3$ (D) $7/10$

16. The number of digits in 20^{301} (given $\log_{10} 2 = 0.3010$) is

- (A) 602 (B) 301 (C) 392 (D) 391

17. If $\sqrt{y} = \cos^{-1} x$ then it satisfies the differential equation

$$(1 - x^2) \frac{d^2 y}{dx^2} - x \frac{dy}{dx} = c \text{ where } c \text{ is equal to}$$

- (A) 0 (B) 3 (C) 1 (D) 2

18. The integrating factor of the differential equation $(1 + x^2) \frac{dy}{dx} + y = e^{\tan^{-1} x}$

- (A) $\tan^{-1} x$ (B) $1 + x^2$ (C) $e^{\tan^{-1} x}$ (D) $\log_e(1 + x^2)$

19. The solution of the equation $\log_{10} \log_7 (\sqrt{x+7} + \sqrt{x}) = 0$ is

- (A) 3 (B) 7 (C) 9 (D) 49

20. Let $f(x)$ be a differentiable function and $f(4) = 5$. Then $\lim_{x \rightarrow 2} \frac{f(4) - f(x)^2}{x - 2}$

- (A) 0 (B) 5 (C) 20 (D) -20

21. The value of $\lim_{x \rightarrow 0} \frac{\int_0^{x^2} \cos(t^2) dt}{x \sin x}$ is
 (A) 1 (B) -1 (C) 2 (D) $\log_e 2$
22. If $\lim_{x \rightarrow 0} \frac{2a \sin x - \sin 2x}{\tan^3 x}$ exists and is equal to 1, then the value of a is
 (A) 2 (B) 1 (C) 0 (D) -1
23. If $f(x) = \begin{cases} 2x^2 + 1, & x \leq 1 \\ 4x^3 - 1, & x > 1 \end{cases}$ then $\int_0^2 f(x) dx$ is
 (A) 47/3 (B) 50/3 (C) 1/3 (D) 47/2
24. The number of solution(s) of the equation $\sqrt{x+1} - \sqrt{x-1} = \sqrt{4x-1}$ is /are
 (A) 2 (B) 0 (C) 3 (D) 1
25. If $\sin^{-1}\left(\frac{x}{13}\right) + \operatorname{cosec}^{-1}\left(\frac{13}{12}\right) = \frac{\pi}{2}$ then the value of x is
 (A) 5 (B) 4 (C) 12 (D) 11

Raf work